Assignment Information

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Tie-Breaking

- In A*, you can have two nodes with the same f-cost
 Which should you prefer?
- What about in WA* and GBFS?



Assignment Format

- Investigating the impact of tie-breaking and reexpansions on A*, WA*, and GBFS
- Given a codebase with A* implemented
 - Will have to add WA* and GBFS
 - Will have to add different tie-breaking rules
 - Will have to add re-expansion options
- Three proofs as well



Re-Expansions

 Comparing WA* and GBFS when you reopen nodes and when you do not



```
def OCL(s_I):
         OPEN \leftarrow \{s_I\}, CLOSED \leftarrow \{\},
        g(s_l) = 0, parent(s_l) = \emptyset

while OPEN \neq \{\}:
                  p \leftarrow SelectNode(OPEN)
                  if p is a goal, return path to p
                  for c \in children(p):
                           if c \notin OPEN \cup CLOSED:
                                    g(c) = g(p) + \kappa(p, c)

parent(c) = p
                                    OPEN \leftarrow OPEN \cup \{c\}
                           else if g(c) > g(p) + \kappa(p,c):
                                    g(c) = g(p) + \kappa(p,c)
                                    parent(c) = p
                                    if c \in CLOSED:
                                             OPEN \leftarrow OPEN \cup \{c\}
                                             CLOSED \leftarrow CLOSED - \{c\}
                  OPEN \leftarrow OPEN - \{p\}, CLOSED \leftarrow CLOSED \cup \{p\}
        return No solution exists
```

```
\begin{aligned} \operatorname{defOCL}(s_l) &: \\ \mathit{OPEN} \leftarrow \{s_l\}, \mathit{CLOSED} \leftarrow \{\}, \\ g(s_l) = 0, \mathit{parent}(s_l) = \emptyset \\ \mathbf{while} \ \mathit{OPEN} \neq \{\} &: \\ p \leftarrow \mathit{SelectNode}(\mathit{OPEN}) \\ \mathbf{if} \ \mathit{p} \ \mathbf{is} \ \mathit{a} \ \mathit{goal}, \mathbf{return} \ \mathit{path} \ \mathit{to} \ \mathit{p} \\ \mathbf{for} \ \mathit{c} \in \mathit{children}(p) &: \\ g(c) = g(p) + \kappa(p, c) \\ \mathit{parent}(c) = p \\ \mathit{OPEN} \leftarrow \mathit{OPEN} \cup \{c\} \\ \mathbf{else} \ \mathbf{if} \ \mathit{g}(c) > g(p) + \kappa(p, c) \\ \mathit{g}(c) = g(p) + \kappa(p, c) \\ \mathit{parent}(c) = p \\ \mathbf{if} \ \mathit{c} \in \mathit{CLOSED} &: \\ \mathit{OPEN} \leftarrow \mathit{OPEN} \cup \{c\} \\ \mathit{CLOSED} \leftarrow \mathit{CLOSED} - \{c\} \\ \mathit{OPEN} \leftarrow \mathit{OPEN} - \{p\}, \mathit{CLOSED} \leftarrow \mathit{CLOSED} \cup \{p\} \\ \mathbf{return} \ \mathit{No} \ \mathit{solution} \ \mathit{exists} \end{aligned}
```

```
def OCL(s_I):
        OPEN \leftarrow \{s_I\}, CLOSED \leftarrow \{\},
        g(s_I) = 0, parent(s_I) = \emptyset
        while OPEN \neq \{\}:

p \leftarrow SelectNode(OPEN)

if p is a goal, return path to p
                 for c \in children(p):
                          if c \notin OPEN \cup CLOSED:
                                   g(c) = g(p) + \kappa(p, c)
                                   parent(c) = p
                                   OPEN \leftarrow OPEN \cup \{c\}
                          else if g(c) > g(p) + \kappa(p, c):
                                   g(c) = g(p) + \kappa(p,c)
                                   parent(c) = p
                                          CLOSED:
                                            OPEN
                                           GEUSED - CLOSED
                 OPEN \leftarrow OPEN - \{p\}, CLOSED \leftarrow CLOSED \cup \{p\}
        return No solution exists
```

```
\mathbf{def} \, \mathsf{OCL}(s_I):
        OPEN \leftarrow \{s_I\}, CLOSED \leftarrow \{\},\
        a(s_t) = 0, parent(s_t) = \emptyset
        while OPEN \neq \{\}:
                 p \leftarrow SelectNode(OPEN)
                 if p is a goal, return path to p
                 for c \in children(p):
                         if c \notin OPEN \cup CLOSED:
                                  g(c) = g(p) + \kappa(p, c)
                                  parent(c) = p
                                  OPEN \leftarrow OPEN \cup \{c\}
                         else if g(c) > g(p) + \kappa(p,c) and
                                           c \in OPEN:
                                  g(c) = g(p) + \kappa(p, c)
                                  parent(c) = p
                 OPEN \leftarrow OPEN - \{p\}, CLOSED \leftarrow CLOSED \cup \{p\}
        return No solution exists
```

Re-Expansions

- Comparing WA* and GBFS when you reopen nodes and when you do not
 - How does this impact performance?



Sliding Tile Puzzle

- Classic grid puzzle where you slide tiles
 - All slides cost 1
- Using Manhattan distance heuristic



Grid Pathfinding

- Pathfinding in a grid
- 4-connected means can move N, E, S, W
 - Every move costs 1
- 8-connected means can also move NE, SE, SW, NW
 - Diagonal moves cost square root 2
- Heuristics
 - Manhattan distance for 4-connected
 - Octile distance for 8-connected



A* Implementation

- Dijkstra's is O(|V|log|V| + |E|)
 - Why?



A* Implementation

- NodeTable for OPEN and CLOSED list
 - Nodes are assigned a StateID
 - Hash table for Open-Closed list checking
- Priority Queue for OPEN list

